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**TITLE**

BOREHOLE SURVEYING

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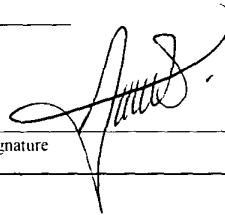
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Date

09/18/03

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1     "Borehole Surveying"

2

3     This invention relates to a method and apparatus for  
4     use in surveying of boreholes.

5

6     It is known in directional drilling, for example, to  
7     detect the orientation of a drillstring adjacent to  
8     the bit by means of a sensor package for determining  
9     the local gravitational **[GX,GY,GZ]** and magnetic  
10    **[BX,BY,BZ]** field components along mutually  
11    orthogonal axes, and to derive from these the local  
12    azimuth **(AZ)** and inclination **(INC)** of the  
13    drillstring. Conventionally, the measurements are  
14    made by providing within the instrument package  
15    three mutually perpendicular accelerometers and  
16    three mutually perpendicular magnetic fluxgates.

17

18    The present invention is concerned with an  
19    arrangement which requires only two measurement  
20    devices, namely a single accelerometer and a single  
21    magnetic fluxgate or a single accelerometer and a  
22    single rate gyro, the latter being preferred for  
23    situations in which magnetic interference is likely  
24    to be encountered.

25

26    Accordingly, the present invention provides a method  
27    of surveying boreholes, comprising:

1        providing an instrument package in the leading  
2        end of a drillstring, the instrument package  
3        comprising first and second single-axis sensors  
4        mounted for rotation with the drillstring about the  
5        rotational axis of the drillstring, the first sensor  
6        being an accelerometer and the second sensor being a  
7        magnetic fluxgate or a rate gyro;

8        rotating the drillstring;

9        deriving from the first sensor the inclination  
10       angle of the drillstring at the instrument package;  
11       and

12       deriving from the second sensor the azimuth  
13       angle of the drillstring at the instrument package.

14  
15       Each of the sensors will typically be positioned in  
16       one of two configurations. In the first  
17       configuration, the sensor is radially spaced from  
18       the borehole axis and has its sensing axis in a  
19       plane containing the borehole axis and an axis  
20       perpendicular thereto. In the second configuration,  
21       the sensor is radially spaced from the borehole axis  
22       and has its sensing axis in a plane parallel with  
23       the borehole axis.

24  
25       Preferably, the drilling control rotation angle is  
26       also obtained from the sensor outputs.

27  
28       Preferably, the sensor outputs are integrated over  
29       the four quadrants of rotation and the desired  
30       output angle is derived from the integrated output.  
31       The instrument package suitably includes rotation  
32       angle reference means for use in the integration.

1  
2 Additional information may be derived, such as the  
3 local gravitational and magnetic field vectors.  
4

5 From another aspect, the invention provides  
6 apparatus for use in surveying boreholes, the  
7 apparatus comprising an instrument package adapted  
8 to be included in the leading end of a drillstring,  
9 the instrument package comprising first and second  
10 single-axis sensors mounted for rotation with the  
11 drillstring about the rotational axis of the  
12 drillstring, the first sensor being an accelerometer  
13 and the second sensor being a magnetic fluxgate or a  
14 rate gyro; and computing means for deriving from the  
15 first sensor while the drillstring is rotating the  
16 inclination angle of the drillstring at the  
17 instrument package, and for deriving from the second  
18 sensor while the drillstring is rotating the azimuth  
19 angle of the drillstring at the instrument package.  
20

21 The computing means preferably operates to integrate  
22 the sensor outputs over the four quadrants of  
23 rotation and to derive the desired output angle  
24 from the integrated output.  
25

26 The apparatus may further include rotation angle  
27 reference means for use in the integration.  
28

29 Examples of the present invention will now be  
30 described, by way of illustration only, with  
31 reference to the drawings, in which:  
32

1           Fig. 1 illustrates, in general terms, the  
2   operation of a single axis sensor in a drillstring  
3   for sensing any given vector  $V$ ;

4           Fig. 2 is a block diagram of one circuit which  
5   may be used to identify rotation quadrant;

6           Fig. 3 illustrates the operation where the  
7   sensor is an accelerometer;

8           Fig. 4 illustrates the operation where the  
9   sensor is a fluxgate;

10          Fig. 5 illustrates the derivation of azimuth  
11   angle; and

12          Fig. 6 illustrates the operation where the  
13   sensor is a rate gyro.

14

15

#### 16   Single-axis sensor

17

18   The operation of a single-axis sensor in a drill  
19   string will first be described in general terms.  
20   The application of this to specific sensors is  
21   discussed below.

22

23   Referring to Fig. 1, a single-axis sensor 10 is  
24   mounted on a drill string (not shown). The sensor  
25   10 senses a fixed vector  $\{V\}$  and is mounted in one  
26   of two configurations.

27

28   In the first configuration, the sensor 10 lies in a  
29   plane containing the rotation axis  $(OZ)$  of the drill  
30   string and axis  $(OX)$  perpendicular to  $(OZ)$ . Axis  
31    $(OY)$  makes up the conventional orthogonal set of  
32   axes  $[OX, OY, OZ]$ . The sensor 10 is mounted at a

1 distance  $r$  from the (OZ) axis and the angle between  
 2 the sensing axis (OS) and the rotational axis (OZ)  
 3 is  $m$ .

4

5 In the second configuration, the sensor 10 is  
 6 mounted in a plane which is parallel to the borehole  
 7 axis (OZ) and with its sensing axis perpendicular to  
 8 the axis (OY) and making angle  $m$  with the direction  
 9 of the borehole axis (OZ).

10

11 If the rate of rotation about the (OZ) axis is  $w$  and  
 12 the components of  $\{V\}$  are  $\{VOZ\}$  along the (OZ) axis  
 13 direction and  $\{VOXY\}$  in the (OXY) plane, then if the  
 14 output from the sensor 10 for both configuration 1  
 15 and configuration 2 of Figure 1 is of the form

16

$$17 \quad V(t) = VOZ.\cos(m) + VOXY.\sin(m).\cos(w.t) + c$$

18

19 where time  $t = 0$  when the axis (OX) is coincident  
 20 with the direction of  $\{VOXY\}$  and  $c$  is constant for  
 21 any fixed rotation rate  $w$ .

22

23 Thus, the sensor output at time  $t$  can be written:

24

$$25 \quad V(t) = K1.\cos(w.t) + K2 \quad \dots\dots\dots(i)$$

26

27 where  $K1 = VOXY.\sin(m)$  and  $K2 = VOZ.\cos(m) + c$  are  
 28 constant if the vector amplitudes  $VOZ$  and  $VOXY$  are  
 29 constant.

30

# Sensor output integration

2

3 The integration of  $V(t)$  from any initial time  $t_i$  to  
 4  $t_i + T/4$ , where  $T = 2\pi/w$ , the time for one  
 5 revolution about (OZ), is

6

$$7 \quad Q = \int_{t_i}^{t_i+T/4} K1.\cos(wt).dt + \int_{t_i}^{t_i+T/4} K2.dt$$

8

9 Thus,

$$10 \quad \begin{array}{rcl} & t_i + T/4 & \\ 11 \quad Q = [(K1/w).\sin(w.t)] & + K2.T/4 & \\ & t_i & \end{array}$$

13

14 or

15

$$16 \quad Q = (K1/w).[\sin(w.t_i + w.T/4) - \sin(w.t_i)] + L$$

17

18 or

$$19 \quad Q = (K1/w).[\sin(w.t_i + \pi/2) - \sin(w.t_i)] + L$$

20 or

$$21 \quad Q = (K1/w).[\cos(w.t_i) - \sin(w.t_i)] + L \quad \dots\dots(ii)$$

22 where  $L$  is a constant  $= K2.T/4$ .

23

24 Using equation (ii), the integration of  $V(t)$  from an  
 25 arbitrary time  $t_0$  to time  $t_0+T/4$  yields

26

$$27 \quad Q1 = (K1/w).[\cos(w.t_0) - \sin(w.t_0)] + L \quad \dots\dots(iii)$$

28

29 Using equation (ii), the integration of  $V(t)$  from  
 30 time  $t_0+T/4$  to time  $t_0+T/2$  yields

31

$$Q2 = (K1/w) \cdot [\cos(w.t0 + w.T/4) - \sin(w.t0 + w.T/4)] + L$$

or

$$Q2 = (K1/w) \cdot [\cos(w.t0 + \pi/2) - \sin(w.t0 + \pi/2)] + L$$

or

$$Q2 = (K1/w) \cdot [-\sin(w.t0) - \cos(w.t0)] + L \quad \dots (iv)$$

6

Using equation (ii), the integration of  $V(t)$  from time  $t0+T/2$  to  $t0+3T/4$  yields

9

$$Q3 = (K1/w) \cdot [\cos(w.t0+w.T/2) - \sin(w.t0+w.T/2)] + L$$

or

$$Q3 = (K1/w) \cdot [\cos(w.t0+\pi) - \sin(w.t0+\pi)] + L$$

or

$$Q3 = (K1/w) \cdot [-\cos(w.t0) + \sin(w.t0)] + L \quad \dots (v)$$

15

Using equation (ii), the integration of  $V(t)$  from time  $t0+3T/4$  to time  $t0+T$  yields

18

$$Q4 = (K1/w) \cdot [\cos(w.t0+w.3T/4) - \sin(w.t0+w.3T/4)] + L$$

or

$$Q4 = (K1/w) \cdot [\cos(w.t0+3\pi/2) - \sin(w.t0+3\pi/2)] + L$$

or

$$Q4 = K1/w \cdot [\sin(w.t0) + \cos(w.t0)] + L \quad \dots (vi)$$

24

Writing  $K = K1/w$  and  $\alpha = w.t0$ , then equations (iii) through (vi) yield for the four successive integrations of  $V(t)$

28

$$Q1 = -K.\sin\alpha + K.\cos\alpha + L \quad \dots (vii)$$

$$Q2 = -K.\sin\alpha - K.\cos\alpha + L \quad \dots (viii)$$

$$Q3 = K.\sin\alpha - K.\cos\alpha + L \quad \dots (ix)$$



$$1 \quad Q4 = K.\sin\alpha + K.\cos\alpha + L \quad \dots\dots\dots(x)$$

2

3 Integration control

4

5 In order to control the sensor output integration,  
 6 as just described, over four successive quarter  
 7 periods of the drill string rotation, a train of **n**  
 8 (with **n** any multiple of 4) equally spaced pulses per  
 9 revolution must be generated. If one pulse **P<sub>0</sub>** of  
 10 this pulse train is arbitrarily chosen at some time  
 11 **t<sub>0</sub>**, the repeated pulses **P<sub>n/4</sub>**, **P<sub>n/2</sub>** and **P<sub>3n/4</sub>** define  
 12 times **t<sub>0</sub>+T/4**, **t<sub>0</sub>+T/2** and **t<sub>0</sub>+3T/4** respectively where  
 13 the period of rotation **T = 2π/w** and **w** is the angular  
 14 velocity of rotation.

15

16 A suitable means for generating an appropriate  
 17 control pulse train is described in US-A1-  
 18 20020078745, which is hereby incorporated by  
 19 reference.

20

21 In an alternative form of integration control, the  
 22 sensor output waveform itself can be used with  
 23 appropriate circuitry for defining the integration  
 24 quadrant periods. In particular, the relatively low  
 25 noise magnetic fluxgate output is well suited to act  
 26 as input to a phase-locked-loop arrangement. Fig. 2  
 27 shows such an arrangement, successive output pulses  
 28 defining the integration quadrants.

29

30 Rotation angle

31

1 Equations (vii) through (x) can be solved to yield  
 2 angle  $\alpha$ ; there is a degree of redundancy in the  
 3 possible solutions but, for example,

$$4 \quad Q1 - Q2 = 2K.\cos\alpha$$

6 and

$$7 \quad Q3 - Q2 = 2K.\sin\alpha$$

8 or

$$9 \quad \sin\alpha/\cos\alpha = (Q3-Q2)/(Q1-Q2) \quad \dots\dots(x_i)$$

10

11 Since  $\alpha = w.t_0$ , the angle  $S(t_0)$  between the axis  
 12 (OX) and the direction of {VOXY} at time  $t_0$  can be  
 13 determined from equation (xi), and the angle between  
 14 (OX) and {VOXY} at any time  $t_m$  measured from the  
 15 arbitrary starting time  $t_0$  is then

16

$$17 \quad S(t_m) = \alpha + w.t_m = S(t_0) + 2\pi.t_m/T \quad \dots(x_{ii})$$

18

19 Magnitudes of vectors {VOXY} and {VOZ}

20

21 Equations (vii) through (x) can be solved to yield  
 22 the constant L:

23

$$24 \quad L = (Q1 + Q2 + Q3 + Q4)/4 \quad \dots\dots(x_{iii})$$

25

26 and the constant K can be determined from:

27

$$28 \quad (K)^2 = [(Q1-L)^2 + (Q2-L)^2]/2$$

$$29 \quad \quad \quad = [(Q3-L)^2 + (Q4-L)^2]/2 \quad \dots(x_{iv})$$

30

31 The magnitude of vector {VOZ} can be determined as

1  
 2  $VOZ = (K2 - c) / \cos(m) = (4.L/T - c) / \cos(m) \quad \dots(xv)$   
 3 provided that constant  $c$  is known.

4  
 5 The magnitude of vector  $\{VOXY\}$  can be determined as

6  
 7  $VOXY = K1 / \sin(m) = (K.w) / \sin(m) \quad \dots\dots(xvi)$

8  
 9 Inclination angle

10  
 11 The inclination angle  $(INC)$  can be derived from the  
 12 gravity vector  $\{G\}$  with the aid of a rotating  
 13 accelerometer.

14  
 15 Referring to Fig. 3, where  $(INC)$  is the angle  
 16 between the tool axis  $(OZ)$  and the gravity vector  
 17  $\{G\}$ ,

18  
 19  $GOZ = G \cdot \cos(INC) \quad \dots(xvii)$

20 and

21  $GOXY = -G \sin(INC) \quad \dots\dots(xviii)$

22  
 23 The accelerometer output can be written as

24  
 25  $VG(t) = GOZ \cdot \cos(m) + GOXY \cdot \sin(m) \cdot \cos(wt)$   
 26  $\quad + CP \cdot \sin(m) + D \cdot \sin(m) \quad \dots\dots(xix)$

27  
 28 where  $CP$  is a centripetal acceleration term and  $D$  is  
 29 a sensor datum term. The centripetal acceleration  
 30 term  $CP$  is zero for configuration 2 and makes this  
 31 the preferred configuration for mounting of the  
 32 accelerometer.

1  
2 Since **CP** is proportional to  $w^2/r$  and is constant for  
3 constant **w**, then clearly **VG(t)** is of the form

4  
5 
$$\mathbf{VG}(t) = K1.\cos(w.t) + K2(w)$$
  
6 (or  $K1.\cos(w.t) + K2$  for configuration 2) ....(**xx**)

7  
8 where **K1** and **K2(w)** are constants at constant angular  
9 velocity **w** in the case of configuration 1 and always  
10 constant in the case of configuration 2. the  
11 constants **K1** and **K2(w)** can be determined from the  
12 accelerometer output integrations as described above  
13 together with the angle (**Highside Angle HS = w.t**)  
14 between the axis (**OX**) and the direction of **{GOXY}**.

15  
16 
$$K1 = GOXY.\sin(m) \quad \dots\dots(xxi)$$

17 and

18 
$$K2(w) = GOZ.\cos(m) + D.\sin(m) \quad \dots\dots(xxii)$$

19 with

20 
$$C(w) = CP.\sin(m) + D.\sin(m) \quad \dots\dots(xxiii)$$

21 constant at constant angular velocity **w** (or for  
22 configuration 2 at all **w**).

23  
24 A calibration procedure can be carried out to  
25 determine the values of **C(w)** for angular velocity  
26 values **w** (constant in the case of configuration 2)  
27 by calculating values of **K2(w)** with the rotation  
28 axis (**OZ**) horizontal when **C(w) = K2(w)**.

29  
30 Thus, for any drilling situation with known angular  
31 velocity **w**, the vector components of the local  
32 gravity vector **{G}** can be determined as

1  
2      $GOXY = K1/\sin(m)$  .....(xxiv)  
3     and  
4      $GOZ = (K2(w) - C(w))/\cos(m)$  .....(xxv)  
5  
6     The inclination angle (INC) can then be determined  
7     from  
8  
9      $\sin(INC)/\cos(INC) = -GOXY/GOZ$  .....(xxvi)  
10  
11     Azimuth angle  
12  
13     When using a rotating fluxgate, the azimuth angle  
14     (AZ) can be determined from a consideration of the  
15     magnetic vector {B}. What follows is applicable to  
16     both configuration 1 and configuration 2.  
17  
18     With reference to Fig. 4, it can be shown that  
19  
20      $BOZ = BV.\cos(INC)$   
21              $+ BN.\cos(AZ).\sin(INC)$  ....(xxvii)  
22  
23     and  
24  
25      $BOXY = (BN.\cos(AZ).\cos(INC) - BV.\sin(INC)).\cos(HS-MS)$   
26              $+ BN.\sin(AZ).\sin(HS-MS)$  .....(xxviii)  
27  
28     or, with  $HS-MS = d$  a constant,  
29  
30      $BOXY = (BN.\cos(AZ).\cos(INC) - BV.\sin(INC)).\cos(d)$   
31              $+ BN.\sin(AZ).\sin(d)$  .....(xxix)  
32

1 With **D** the fluxgate datum, the fluxgate output can  
 2 be written

$$3 \quad \text{VB}(t) = \text{BOZ}.\cos(m) + \text{BOXY}.\sin(m).\cos(w.t) \\
 4 \quad \quad \quad + \text{D}.\sin(m) \quad \quad \quad \text{.....(xxx)}$$

6 or

$$7 \quad \text{VB}(t) = \text{K1}.\cos(w.t) + \text{K2} \quad \quad \quad \text{.....(xxxi)}$$

8 where

$$9 \quad \text{K1} = \text{BOXY}.\sin(m)$$

10 and

$$11 \quad \text{K2} = \text{BOZ}.\cos(m) + \text{D}.\sin(m) \\
 12 \quad \quad = \text{BOZ}.\cos(m) + \text{C} \quad \quad \quad \text{.....(xxxii)}$$

13  
 14 are constants which can be determined from the  
 15 fluxgate output integrations as described above  
 16 together with the angle (**Magnetic Steering Angle =**  
 17 **MS = w.t**) between the axis (**OX**) and the direction of  
 18 **{BOXY}**.

19  
 20 A calibration procedure can be carried out to  
 21 determine the value of the constant **C** by calculating  
 22 the value of **K2** while rotating about the direction  
 23 of the axis (**OZ**) along which **BOZ = 0** when **K2 = C**.

24  
 25 Thus, for any drilling situation the vector  
 26 components of the local magnetic field **{B}** can be  
 27 determined as

$$28 \quad \text{BOXY} = \text{K1}/\sin(m) \quad \quad \quad \text{.....(xxxiii)}$$

30 and

$$31 \quad \text{BOZ} = (\text{K2}-\text{C})/\cos(m) \quad \quad \quad \text{.....(xxxiv)}$$

32

1 With reference to Fig. 5, the horizontal component  
 2 **{BN}** of the local magnetic field vector **{B}** can be  
 3 represented by horizontal components **{B1}** and **{B2}**  
 4 where

$$\begin{aligned} 5 \\ 6 \quad B1 &= BOXY.\cos(d).\cos(INC) \\ 7 \quad &\quad + BOZ.\sin(INC) \quad \dots\dots(xxxv) \end{aligned}$$

8 and

$$9 \quad B2 = BOXY.\sin(d) \quad \dots\dots\dots(xxxvi)$$

10

11 The Azimuth Angle (**AZ**) can then be determined from

$$12 \\ 13 \quad \sin(AZ)/\cos(AZ) = -B2/B1 \quad \dots\dots\dots(xxxvii)$$

14

15 Also, the horizontal component of the local magnetic  
 16 field can be determined from

$$17 \\ 18 \quad BN = (B1^2 + B2^2)^{3/2} \quad \dots\dots\dots(xxxviii)$$

19

20 and the vertical component of the local magnetic  
 21 field can be determined from

$$\begin{aligned} 22 \\ 23 \quad BV &= BOZ.\cos(INC) \\ 24 \quad &\quad - BOXY.\cos(d).\sin(INC) \quad \dots\dots(xxxix) \end{aligned}$$

25

26 Earth's rotation vector

27

28 Where it is not practicable to use a magnetic  
 29 fluxgate, this may be replaced by a rate gyro as  
 30 sensor.

31

1 With reference to Fig. 6, if the geographic latitude  
 2 at the drilling location is **(LAT)** then the vertical  
 3 component of the earth's Rotation Vector **{RE}** is

4

$$5 \quad \mathbf{RV} = -\mathbf{RE}.\sin(\mathbf{LAT}) \quad \text{.....}(\mathbf{x1})$$

6 and the horizontal component is

$$7 \quad \mathbf{RN} = \mathbf{RE}.\cos(\mathbf{LAT}) \quad \text{.....}(\mathbf{xli})$$

8

9 The magnitude of the cross-axis rate vector **{ROXY}**  
 10 can be shown to be

11

$$12 \quad \mathbf{ROXY} = (\mathbf{RN}.\cos(\mathbf{GAZ}).\cos(\mathbf{INC}) - \mathbf{RV}.\sin(\mathbf{INC})).\cos(\mathbf{d})$$

$$13 \quad \quad \quad + \mathbf{RN}.\sin(\mathbf{GAZ})\sin(\mathbf{d}) \quad \text{.....}(\mathbf{xlii})$$

14

15 where **(GAZ)** is the gyro azimuth angle and

16 **d = HS - GS** is constant.

17

18 Since **RN**, **RV**, **d** and **INC** are known and **ROXY** can be  
 19 derived as discussed below, **(GAZ)** can be determined.

20

21 With the particular configuration where the rate  
 22 gyro sensing axis is perpendicular to the drill  
 23 string rotation axis **(OZ)**, the rate gyro output can  
 24 be written

25

$$26 \quad \mathbf{VG}(t) = \mathbf{ROXY}.\cos(\mathbf{w.t}) + \mathbf{D} \quad \text{.....}(\mathbf{xliii})$$

27

28 where **D** is the rate gyro datum, or

29

$$30 \quad \mathbf{VG}(t) = \mathbf{K1}.\cos(\mathbf{w.t}) + \mathbf{K2} \quad \text{.....}(\mathbf{xliv})$$

31



1 where the constant **K1 = ROXY** can be determined from  
2 the rate gyro output integrations as described above  
3 together with the Gyro Steering Angle **GS = w.t**  
4 between **(OX)** and the direction of **{ROXY}**.

5  
6 The variation in the Rate Gyro Datum makes it  
7 difficult to achieve satisfactory datum calibration  
8 in all circumstances. It is unlikely that Gyro  
9 Azimuth measurements should be attempted at high  
10 inclination angles. The use of the rate gyro is  
11 most likely with near-vertical boreholes in  
12 locations where magnetic azimuth measurements are  
13 unreliable (such as close to rigs) and the Gyro  
14 Azimuth **GAZ** is approximately equal to the angle **d**.

15  
16 The present invention thus makes possible the  
17 measurement of a number of borehole-related  
18 parameters during rotation of a drillstring and  
19 using a reduced number of sensors. Modifications  
20 may be made to the foregoing embodiments within the  
21 scope of the present invention.